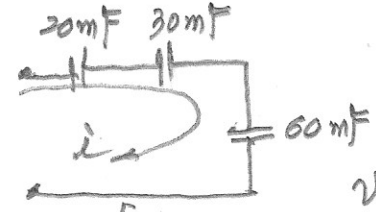
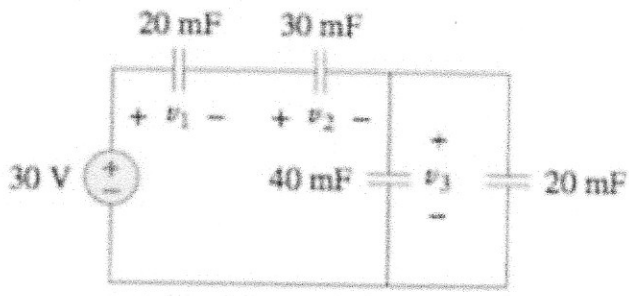


solve

EE101 Quiz 6 February 21, 2017

Name _____ Student ID _____

Find the voltage across the 40 mF capacitor and also the energy stored in it.



$$30V = \left(\frac{1}{20mF} + \frac{1}{30mF} + \frac{1}{60mF} \right) Q$$

$$v_k = \frac{1}{C_k} \int i(t) dt = \frac{1}{C_k} Q$$

$$Q = \frac{30}{\frac{1}{20mF} + \frac{1}{30mF} + \frac{1}{60mF}}$$

$$V_3 = \frac{Q}{60mF} = \frac{30}{3+2+1} = 5V$$

$$E_3 = \frac{1}{2} C V^2 = \frac{1}{2} \times 40 \times 10^{-3} \times 5^2 = 0.5 J$$

Your answer $v_3 =$ 5 V [7 points]

Energy $E_3 =$ 0.5 Joule [J] [3 points]

Hint: charges stored in capacitors in series are same since

- $q(t) = \int_{-\infty}^t i(\tau) d\tau$
- First calculate C_{eq} seen by the 30V source. (3 points) $C_{eq} = \frac{10}{5} mF$
- Next find the q 0.3 C (2 points), then $v_3 =$ 5 V (2 points)
- Energy (3 points) $E_3(t) = \int_{-\infty}^t v_3 \cdot ((40 mF) \frac{dv_3}{dt}) d\tau$

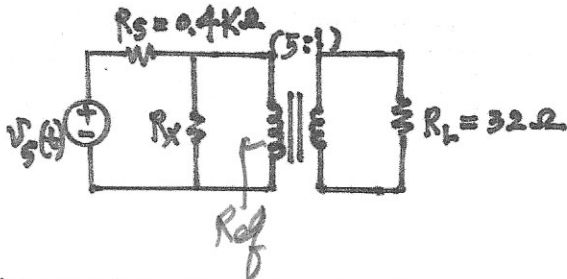
$$q = C V = 10 mF \cdot 30V = 0.3 C$$

$$= 40mF \cdot \frac{5^2}{2} = 40mF \times \frac{(5)^2}{2} = 0.5 C$$

solve

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This problem is to make sure a maximum power transfer is achieved by matching the resistance value (or an equivalent resistance) on the power generation side to the load resistance. The problem is made more interesting with use of a transformer with its turn ratio 5:1 between the load and the power generation side.



Q1 (6 points) Find the value of R_x for maximum power transfer for to R_L .

$$R_{ref} = 32 \times 5^2 = 32 \times 25 = 800 \Omega$$

For max power, $R_s = 0.4 k\Omega = R_x \parallel R_{ref} = R_x \parallel 800 \Omega$
 $\Rightarrow R_x = 800 \Omega$

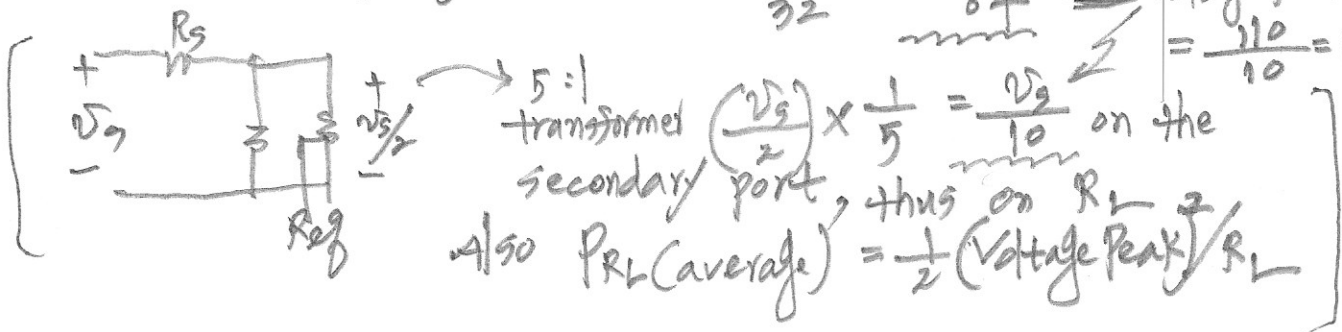
Q2 (4 points) Calculate the average power delivered to R_L when the voltage source is

$$v_s(t) = 110 \sin \omega t \text{ [v]}, \text{ where } \omega = 2\pi \times 60 = 120 \pi.$$

voltage across $R_L = \frac{V_s}{10}$

$$P_{R_L} = \frac{1}{2} \frac{(110)^2}{32} = \frac{1}{2} \frac{(11)^2}{32} = \frac{121}{64} = 1.89 \text{ W}$$

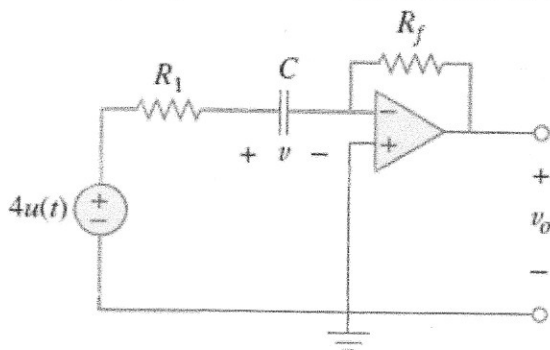
voltage peak
 $= \frac{110}{10} = 11 \text{ V}$



90/ve

Name _____ Student ID _____

For the op amp circuit of the given figure, let $R_1 = 10 \text{ k}\Omega$, $R_f = 30 \text{ k}\Omega$, $C = 90 \text{ }\mu\text{F}$, and $v(0) = 1 \text{ V}$.



- a) (4 points) Write down an equation to find $v(t)$ for the given input voltage $4u(t)$, where $u(t)$ is a step function whose value is 1.0 for $t > 0$, and 0 for $t < 0$.

$$R_1 \left[C \frac{dv(t)}{dt} \right] + v(t) = 4u(t), \quad t > 0$$

$$(10 \text{ k}\Omega \cdot 90 \text{ }\mu\text{F}) \frac{dv(t)}{dt} + v(t) = 4u(t)$$

$$0.9 \frac{dv}{dt} + v = 4u(t) = 4, \quad t > 0$$

- b) (4 points) Solve for $v(t)$ $t > 0$. Verify your solution by checking $v(0)$ and $v(\infty)$.

$$0.9 dv = (4 - v) dt$$

$$\frac{-0.9 d(4-v)}{4-v} = dt$$

$$-0.9 \ln(4-v) \Big|_{v(0)}^v = t \Big|_0^t$$

$$-0.9 \ln \frac{(4-v)}{(4-1)} = t$$

$$\left[\begin{aligned} -0.9 \ln \frac{4-v}{3} &= t \\ \ln \frac{4-v}{3} &= -\frac{t}{0.9} \\ \frac{4-v}{3} &= e^{-\frac{t}{0.9}} \end{aligned} \right]$$

$$e^{-\frac{t}{0.9}} \rightarrow 4-v = 3e^{-\frac{t}{0.9}}$$

- c) (2 points) What is the output voltage v_o $t = \infty$.

At $t = \infty$, the current through R_f is zero,

thus $v_o = R_f \cdot 0 = 0$ ans

ans $v = 4 - 3e^{-\frac{t}{0.9}}$
 $v(0) = 4 - 3 \cdot 1 = 1 \checkmark$
 $v(\infty) = 4$